

# Review on Wavelet Denoised Value at Risk and Application on Crude Oil Market

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**Abstract** Oil markets are more competitive and volatile than ever before. This places the accurate and reliable measurement of market risks in the crucial position for both investment decision and hedging strategy designs. This paper attempts to measure risks in the oil market using Value at Risk (VaR) theory. To estimate VaR at higher accuracy and reliability, this paper proposes Wavelet Denoised Value at Risk (WDNVaR) estimates and compared with classical ARMA-GARCH approach. Performances of both approaches have been tested and compared using Kupiec backtesting procedures. Empirical studies of the proposed Wavelet Denoised Value at Risk (WDNVaR) have been conducted on two major oil markets (I.e. WTI & Brent). Experiment results confirm that WDNVaR improves the accuracy and reliability of VaR estimates over traditional ARMA-GARCH approach significantly, which results from its capability to clean up the data and alleviate distortions introduced by outliers.

**Keywords:** Value-at-Risk, crude oil, ARMA-GARCH, Wavelet, Wavelet Denoised VaR, Kupiec Backtesting procedures

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## 1. Introduction

Crude oil markets can be volatile and risky. The world crude oil prices have risen dramatically during the past decade. However, oil prices did not sustain a constant rise – rather, they showed high volatility, reflecting market conditions such as political turmoil, supply disruptions, unexpected high demand and speculation.

Oil markets have long been the most volatile ones since shocks and the associated risks of losses could prevail in the market due to low inventory level hindered by extremely high storage costs. As the role of market forces increase continuously with the shifts of market from more managed market agreement to the more flexible market based environment, market is getting more volatile and vulnerable to unexpected extreme events [1]. Thus proper measurement and management of market risks are increasingly valued by investors to protect themselves against adverse market movements.

This paper investigates the risk measurement issue in oil markets. The measurement of risks in oil markets are complicated processes since oil prices receive joint influences from numerous risk factors. To name just a few, these may include economic aspects, weather changes, political aspects, military, natural disasters, market sentiments and speculations, etc [2,3].

Value at Risk (VaR), as the latest development in the risk management field, is adopted in this paper to quantify and measure market risks. VaR estimates the potential loss from market risk across an entire portfolio, using probability

concepts by identifying the portfolio containing fundamental risks, allowing an underlying quantifiable and manageable risk factors decomposition of this latter.

Standard VaR estimates take the mathematical form as in equation (1), which means “we are  $\alpha$  percent certain that we will not lose more than  $r_{VaR}$  of our investment in the next  $t$  days under normal market conditions [4]:

$$p\{L(0) - L(t) \leq -r_{VaR}\} = 1 - \alpha \quad (1)$$

Where,  $L(t)$  denotes the value of the portfolio at time  $t$  and  $\alpha$  is the confidence level.

Several methods for VaR estimation have mainly been tried through the following three approaches:

The parametric approach, also called variance-covariance approach is more popular than its more complex and sophisticated non-parametric counterpart, the simulation approach. This approach, implemented as either historical simulation or Monte Carlo simulation, is computationally demanding and very costly as well. When the approach is parametric, it is based on the assumption that returns are distributed normally. The parametric approach is flexible, easy to understand and widely accepted [5].

However, it relies heavily on the assumption of a normal return distribution. The non parametric approach lets the data speak for it self and extends historical patterns hidden in the data into future. Semi parametric emerges recently to strike the balance between the two extremes, where different techniques borrowed from other disciplines, such as engineering, computer science, applied mathematics, etc., made their way into the field of

finance. These may include methods such as Extreme Value Theory, Wavelet Transformation, Fuzzy Logic, etc.

Therefore, this paper proposes wavelet denoising technique to be integral part of VaR estimation process. The original data series are projected into time scale domain. Signals above certain threshold levels are repressed separately. Then VaR is estimated based on better behaved data after denoising process.

Empirical studies based on the proposed Wavelet Denoising VaR (WDNVaR) algorithm & more traditional ARMA-GARCH approach is conducted in both WTI and Brent oil markets. Experiment results are backtested and compared using Kupiec backtesting procedures to evaluate their accuracy and reliability [6]. Incorporating the flexibility of ex ante hybrid algorithm and details analysis in time scale domain offered by wavelet analysis, WDNVaR is found to improve the reliability of VaR estimates and offer greater flexibility than traditional ARMA-GARCH approach.

The organization of this paper develops as follows: The second section reviews of evaluation methods of model based VaR, its potential applications in economics and finance field and wavelet denoising techniques. The third section proposes the wavelet denoised VaR algorithm (WDNVaR). The fourth section applies the proposed WDNVaR and the traditional ARMA-GARCH approach to measure market risk exposure levels in Oil markets and compares model reliability using Kupiec backtesting procedures. The fifth section concludes.

## 2. Literature Review

### 2.1. Evaluation Methods of Model-based VaR

The main works in this field are the ones of Kupiec [7], Christoffersen [8] and Lopez [9] who proposed, respectively, a statistical based procedure and a loss function approach to test if the VaR estimates are correct and consistent with the data.

Two different approaches are actually available to evaluate the VaR estimates: statistical based procedures, and loss functions approaches. The proportion Failure test (or Unconditional coverage test), the time Until First test of Kupiec [7] and the Conditional coverage test of Christoffersen [8] and Lopez [9] belong to the first group belong, while the approach of Lopez [9] belong to the second one. The main difference between the two is that with statistical procedure, inference analysis is available. The test of Kupiec and Christoffersen are based on likelihood ratios, and on the assumption that VaR should exhibit a conditional or unconditional coverage equal to  $p$ .

Among various hypothesis based backtesting procedure available, the one proposed by Kupiec [7] is the simplest and the most popular and available. It is based on the simple notion that the model validation process can be treated as a series of Bernoulli trials testing sequences of success and failure. VaR exceedance  $N$  in large sample  $T$  should converge to the binomial distribution. The likelihood ratio statistics is developed by Kupiec as in equation (2) for testing the specific confidence intervals.

$$LR_{uc} = -2 \log \left[ (1-p)^{T-N} p^N \right] + 2 \log \left\{ \left[ 1 - \left( \frac{N}{T} \right) \right]^{T-N} \left( \frac{N}{T} \right)^N \right\} \quad (2)$$

Where,  $LR_{uc}$  denotes the test statistics that has an asymptotic  $\chi^2(1)$  distribution.  $T$  is the total number of observations that are used in test set.  $p$  is the probability of a VaR exceedance occurrence.

### 2.2. Wavelet in Finance and Economics

The application of wavelet analysis in economic and financial data analysis is only recent phenomenon. Since wavelet analysis projects data signals into time scale domain for analysis, it can be treated as promising multi scale analysis, noise reduction and multi scale modelling tool.

Ramsey [10] gives an overview of the contribution of wavelets to the analysis of economic and financial data. The ability to represent highly complex structures without knowing the underlying functional form proved to be a great benefit for the analysis of these time-series. In addition, wavelets facilitate the precise location of discontinuities and the isolation of shocks.

Furthermore, the process of smoothing found in the time-scale decomposition facilitates the reduction of noise in the original signal, by first decomposing the signal into the wavelet components, then eliminating all values with a magnitude below a certain threshold and finally reconstructing the original signal with the inverse wavelet transform.

Stevenson [11], for example, use wavelet analysis for the filtering of spot electricity prices in the deregulated Australian electricity market. By examining both the demand and price series at different time locations and levels of resolution, Stevenson was able to reveal what was signal and what was noise.

Ramsey and Lampart [12] use wavelet analysis for time-scale decomposition. They researched both the relationships between consumption and income and money and GDP. The time-scale decomposition yielded a new transformed signal built up from the several wavelet coefficients representing the several scales. At each scale, a regression was made between the two variables.

Chew [13] research the relationship between money and income, using the same technique of wavelet-based time-scale decomposition as Ramsey and Lampart [12] did. This research yielded a greater insight in the money versus income nexus in Germany.

Arino [14] use wavelet-based time-scale decomposition for forecasting applications. The approach used was to apply forecasting methods on each of the resulted coefficients from the time-scale decomposition. After applying forecast methods on each of these coefficients, the final forecast of the complete series was obtained by adding up the individual forecasts.

Aussem and Murtagh [15] use neural networks to examine the individual coefficients. The trained neural network with its approximated variables in the target function was used for the final forecast. In the area of

finance, multi-resolution analysis appears useful, as different traders view the market with different time resolutions, for example hourly, daily, weekly or monthly. The shorter the time-period, the higher the frequency. Different types of traders create the multi-scale dynamics of time-series.

Struzik [16] applies the wavelet-based effective Holder exponent to examine the correlation level of the Standard & Poor's index locally at arbitrary positions and resolutions (time and scale).

Norsworthy et al. [17] apply wavelets to analyze the relationship between the return on an asset and the return on the market portfolio, or investment alternative. Similar to other researches in the field of finance and economics, they applied wavelet-based time-scale decomposition to investigate whether there are changes in behavior for different frequencies. The research indicated that the effect of the market return on an individual asset's return will be greater in the higher frequencies than in the lower.

## 2.3. Wavelet Denoising Techniques

### A. Basic Denoising

Denoising, or noise reduction, is a permanent topic for engineers and applied scientists. The problem of denoising is quite varied due to variety of signals and noises. This article considers deterministic signals in zero-mean white noise, as  $y(n)$  in (3):

$$x(t) = s(t) + n(t) \quad (3)$$

Where  $s(t)$  is the signal to be estimated, and  $n(t)$  is a zero mean white noise with variance  $\sigma^2$ . To be exact, the problem is to estimate  $x(t)$ , or denoise  $y(t)$ .

It is always tempting to reduce noise after some kind of signal transformation. An appropriate transform can project signal to a domain where the signal energy is concentrated in a small number of coefficients. If noise, on the other hand, is evenly distributed across this domain, this domain will be a very nice place to do denoising, for the Signal- Noise Ratio (SNR) is greatly increased in some important coefficients, or, the signal is highlighted in this domain while the noise is not.

In this sense, for signals composed with a number of sinusoids, it is wise to denoise in frequency domain. Similarly, for piece-wise constant signals or piecewise polynomial signals, it is advantageous to reduce noise in Wavelet transform domain, or time-scale domain, where these signals have a very sparse representation. Since a wide range of signals can be classified into piece-wise polynomial, Wavelet transform has become an essential tool for many applications, especially image processing.

### B. Hard and Soft Thresholding

Thresholding noisy information using wavelet denoising techniques requires the selection of the thresholding rule and the selection of threshold level, i.e. the thresholding rule must be chosen to govern model reaction to the noisy signals spotted. Furthermore, the threshold selection rule must be set to determine what type of signals is recognized as noise.

Let  $W(\cdot)$  and  $W^{-1}$  denote the forward and inverse wavelet transform operators. Let  $D(\cdot, \lambda)$  denote the

thresholding operator with threshold  $\lambda$ . The practice of thresholding denoising consists of the following three steps:

$$Y = W(x) \quad (4)$$

$$Z = D(Y, \lambda) \quad (5)$$

$$\hat{x} = W^{-1}(Z). \quad (6)$$

Hard thresholding and soft thresholding are only different in step 3. The hard-thresholding function chooses all wavelet coefficients that are greater than the given threshold  $\lambda$  and sets the others to zero.

$$D(Y, \lambda) = \begin{cases} Y & \text{if } |Y| \geq \lambda \\ 0 & \text{otherwise} \end{cases} \quad (7)$$

The threshold  $\lambda$  is chosen according to the signal energy and the noise variance  $\sigma^2$ . The soft-thresholding function has a somewhat different rule from the hard-thresholding function. It shrinks the wavelet coefficients by  $\lambda$  towards zero.

$$D(Y, \lambda) = \begin{cases} Y - \lambda & \text{if } Y \geq \lambda \\ 0 & \text{if } |Y| < \lambda \\ Y + \lambda & \text{if } Y \leq -\lambda \end{cases} \quad (8)$$

The ultimate goal of thresholding is to set the noisy level to the volatility level of the underlying noisy signals. Under that ideal situation, noisy signals are completely wiped out without losing the useful information. However, since the true value of future volatility may never be known for sure, the determination of appropriate thresholding value is a very tricky task. Various threshold selection rules emerge over years including universal thresholding, minimax estimation, Stein's Unbiased Risk Estimate (SURE), etc.

The universal threshold sets threshold level as in (9)

$$\eta^U = \hat{\sigma} \sqrt{2 \text{Log} N} \quad (9)$$

Where  $\eta^U$  is the threshold set,  $N$  is the number of observations and  $\hat{\sigma}$  is the volatility estimator. When  $N$  approaches infinity (i.e. infinitely large sample size), universal threshold guarantees the elimination of all noisy signals. But it may also suppress the true signals when threshold value is set at an overly high level [18].

Therefore, although universal thresholded signals are visually appealing, it is not particularly popular due to its low goodness of fit [19].

Minimax estimation develops as a step forward beyond universal threshold. It shifts the focus from reducing the maximum possible noisy signals to achieving the best function fit. Minimax estimation attempts to attain the minimax value. It minimizes the overall mean square error and retains the maximum level of information possible in the signal. Therefore abrupt changes and spikes usually smoothed or distorted in the universal threshold method are retained in the minimax approach [19,20,21].

### 3. Wavelet Denoised VaR (WDNVaR)

#### 3.1. WDNVAR Theory

Estimating a signal that is corrupted by additive noise has been of interest to many researchers for practical as well as theoretical reasons. The problem is to recover the original signal from the noisy data. The basic principle of wavelet denoising is to identify and zero out wavelet coefficients of the signal which are likely to contain mostly noise. By identifying and preserving significant coefficients, wavelet thresholding preserves important high pass features of the signal such as discontinuities. This property is useful, for example, in image denoising to maintain the sharpness of edges in the image.

Therefore, it's important for the data to be pre-processed before being modelled using conventional VaR estimation approach.

While Fourier transform could also be argued as the algorithm of choice for de-noising process, it is only applicable when the composition of the original process can be well approximated by sinusoidal functions. This requires that the underlying processes are both periodic and globally stationary. However, for financial time series, global stationarity and periodicity are very strong assumptions and rarely hold in practice [18]. Therefore, wavelet analysis is proposed as a more appropriate alternative to capture in the time-frequency domain the non stationarity and non periodicity.

Given wavelet's advantage in locking in details in time frequency domain, it is an extremely useful tool in analyzing and adapting to unknown data characteristics. Typically for financial data, noise level over time and variance corresponding to individual time horizon are unknown. By utilizing the power of wavelet analysis, these data characteristics can be analyzed and manipulated to improve VaR estimation accuracy. After data denoising process, the disturbing noisy signals (such as common white noise) can be filtered out.

Also the signals with the strongest energy concentration can be singled out. Signals that are too weak or possess the least amount of useful information are simply ignored. Therefore, the signal after de-noising process is expected to comply with investors' interests. It is also more stationary and more suitable for model fitting. Thus, wavelet is expected to help in filtering and cleaning noisy signals and data outliers. This prepares better behaved data. Model fitting process is also less affected by those trivial details and outliers [18,22].

The basic procedure for performing wavelet de-noising is as follows: Firstly transform the original signal using wavelet multiresolution analysis. For all the wavelet coefficients at different scales, set a threshold value and set all the wavelet coefficients that have magnitude less than the threshold value to zero [22] and [19,21]. Then WDNVaR is estimated by applying conventional approaches to the denoised data set.

#### 3.2. WDVaR Framework

The basic procedure for performing wavelet de-noising is as follows:

1. By applying wavelet transformation to return series data, the original data are decomposed into sub return series data at different scales J as in (10):

$$r_t = r_{t,A^J} + \sum_{i=1}^J r_{t,D^i} \quad (10)$$

Where,  $r_{t,A^J}$  Decomposed return series by applying scaling function at scale J and Decomposed return series by applying wavelet function at scale i

2. Wavelet coefficients are denoised

- The chosen threshold setting (The universal threshold sets)
- The chosen removing strategy (hard or soft).

3. Denoised data are reconstructed from denoised wavelet coefficients.

- The conditional mean is aggregated from individual forecasts for both denoised data and noises through ARMA model.

$$\hat{\mu}_{aggregated} = \hat{\mu}_{denoisedData} + \hat{\mu}_{noises} \quad (11)$$

- The conditional volatility is aggregated from individual forecasts for both denoised data and noises through GARCH model.

$$\hat{\sigma}_{aggregated}^2 = \hat{\sigma}_{denoisedData}^2 + \hat{\sigma}_{noises}^2 \quad (12)$$

This is done based on the preservation of energy property in wavelet analysis.

4. Then VaR based on wavelet denoised approach is as follows:

$$WDNVaR_t = -a\hat{\sigma}_{WDNVaR,t} - \hat{\mu}_t \quad (13)$$

## 4. Empirical Analysis

In this section we present the data set, the descriptive statistics, forecast performance results and the interpretations of experiments results.

### 4.1. Data Description and Preliminary Analysis

The crude oil is one of the most important industry inputs and remains the major sources of world's energy consumption. The price paths of crude oil and its volatilities affect different market movements and the economic status as a whole [1,23].

West Texas Intermediate (WTI) and Brent (or Brent-Forties-Oseberg) crude oil spot prices are used in this study. These markets are considered the world marker crude oil markets. Most other crude oil prices are related to them.

The covered period is: from 20th May, 1988 to 29th December, 2006 (for Brent crude oil) and from 27th March, 1987 to 30th December, 2005 (for WTI crude oil) respectively. 60% of the data set serves as the training set, while the remaining 40% of the data set is used as the test set. One step ahead out of sample forecast is conducted to evaluate the accuracy and reliability of various models under investigation.

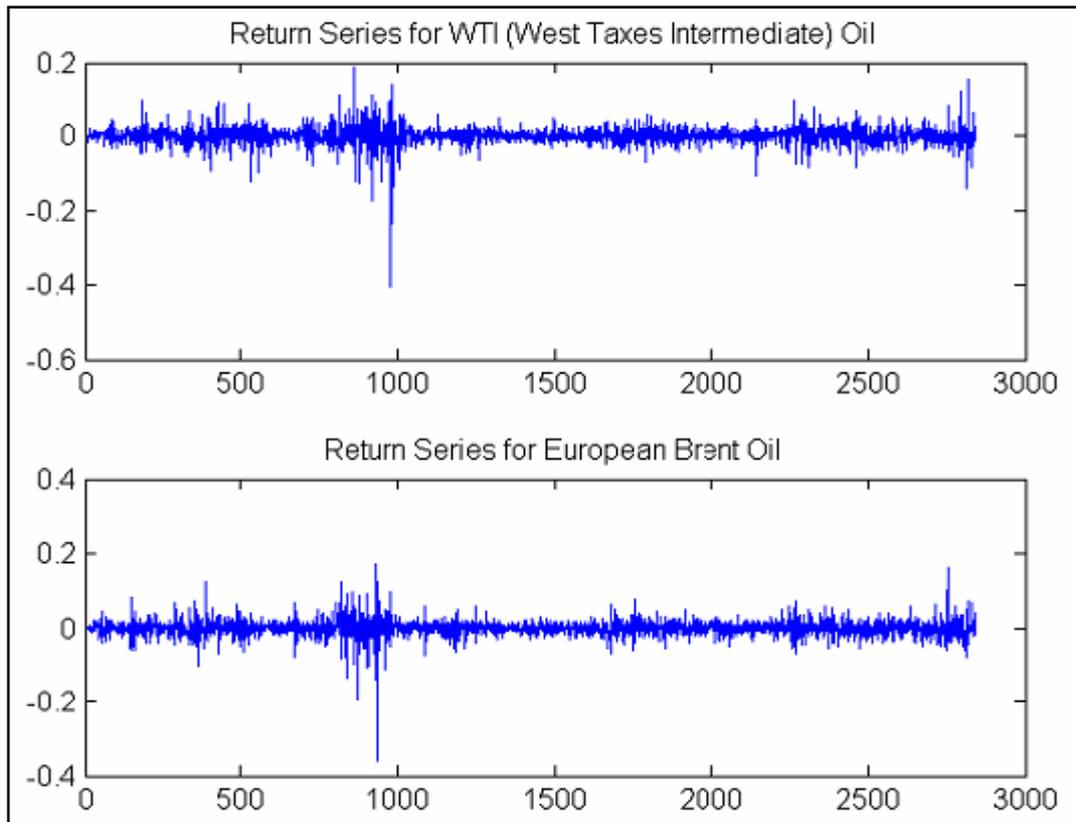


Figure 1. Return series for the two oil markets

During implementation, the training set is continuously expanded to include the newly available observation at each iteration, so that the arrival of new information is taken into consideration. A portfolio of one asset position worth \$1 is assumed for each market. The original observations are log differenced (i.e.  $\log(x_t) - \log(x_{t-1})$ ) for further processing and modelling attempts. Figure 1 displays the return series for WTI and European Brent oil.

## 4.2. Descriptive Statistics

The oil markets are characterized by high volatility and the leptokurtic phenomenon (i.e. fat tail and high kurtosis, which signals high probability of extreme events occurrences), which makes adequate risk management and control necessary. This is confirmed by several stylized facts concluded from Table 1:

Table 1. Descriptive Statistics

Oil Markets	WTI (West Texas Intermediate)	Brent
Mean	-0.00015	-0.00013
Maximum	0.1894	0.1765
Minimum	-0.4103	-0.3512
Standard deviation	0.0316	0.0304
Skewness	-1.7353	-0.3095
Kurtosis	37.9632	33.1282
Jarque-Bera test (p-value)	0	0
BDS Test (p value)	0	0

We remark that these facts suggest a highly competitive and volatile market which makes adequate risk management and control necessary. Firstly, there are significant price

fluctuations in the markets as suggested by positive standard deviations. The substantial difference between the minimum and maximum level also indicates considerable losses if risks are not properly measured and managed.

Secondly, we can remark that there is a higher probability of losses in the second and the fourth market as indicated by the negative Skewness.

Thirdly, the high level of excess kurtosis suggests that the markets are volatile, with high probability of extreme events occurrences.

The nonlinear and volatile nature of the oil markets are further confirmed by formal statistical tests conducted. The rejection of Jarque-Bera test of normality suggests that the returns deviate from normal distribution significantly and exhibit leptokurtic behaviors. The rejection of BDS (Brock-Dechert-Scheinkman) test of independence indicates the existence of non-linearity within the data.

## 4.3. Forecast Performance Results

For hypothesis testing approach, the null hypothesis suggests that the VaR models exhibit statistical properties that are characteristics of accurate VaR estimate. The test statistics is calculated and compared to critical values corresponding to certain confidence level to decide whether or not to reject the model at that confidence level.

## 4.4. Backtesting Results for ARMA-GARCH-VaR

In this paper, traditional hybrid algorithm based on ARMA-GARCH model serves as the benchmark model [24]. The usual ARMA( $r, m$ )-GARCH ( $p, q$ ) takes the form as in (14):

- ARMA(r,m):

$$r_t = C + \sum_{i=1}^R \phi_i r_{t-i} + \sum_{j=1}^M \theta_j \varepsilon_{t-j} + \varepsilon_t \quad (14)$$

$\phi$  : The autoregressive coefficient

$\theta$  : The moving average coefficient;

$\varepsilon$  : The white noise.

- GARCH(1,1):

$$\sigma_t^2 = \omega + \alpha r_{t-1}^2 + \beta \sigma_{t-1}^2$$

$\sigma_t^2$  : The conditional variance at time t.

$\sigma_{t-1}^2$  : The lag 1 variance.

$r_{t-1}^2$  : The lag 1 squared return in the previous period.

Among various parametric models available, hybrid ARMA model with GARCH error correction is widely accepted in both academic and industries since it's easy to understand and implement in practice. But its performance is constrained by its sequential linear filtering process as described before.

The GARCH (1, 1) model is used in the experiment since empirical researches suggested that it suffices for most of the situations. The training set is used to estimate parameters  $\alpha, \beta, \omega$  by maximizing the maximum likelihood equation.

As suggested by experiment results in Table 2, ARMA(1,1)-GARCH(1,1) performs rather well. It only fails at 95% confidence level in WTI oil market and is accepted under all other circumstances.

The performance of ARMA(1,1)-GARCH(1,1) gradually deteriorates under higher confidence levels for all markets. ARMA(1,1)-GARCH(1,1) provides much better coverage of risks under lower confidence level. This implies that ARMA(1,1)-GARCH(1,1) model may underestimate risk measurement and serve as a generally aggressive risk measures.

The high level of acceptance of ARMA-GARCH VaR supports and confirms the popularity of linear combining power of ARMA and GARCH models during the estimation process. However, increasing competition in the markets pushes operators to work on slight margins, implying that additional accuracy and flexibility have to be pursued.

#### 4.5. Backtesting Results for WDNVaR (DB2, 2)

Several parameters for wavelet de-noising process are chosen according to investor's preferences. In this experiment, hard thresholding rule with minimax thresholding is adopted. Wavelet decomposition level is set at level 2 and Daubechies 2 is chosen as the wavelet family.

The return series in the training set is decomposed using the selected wavelet family. Wavelet coefficients at different scales are de-noised according to the chosen thresholding rule and the threshold selection rules. The return series after de-noised process is reconstructed from the de-noised wavelet coefficients. The future daily volatilities are forecasted using estimated ARMA-GARCH model based on the rolling-window method and daily VaR values are forecasted correspondingly.

Experimental results in Table 3 confirm the significant performance improvement gained. WDNVaR is accepted across all markets at 95% confidence levels. During WDNVaR estimation process, ARMA-GARCH model seems to capture more of the data features when applied to wavelet denoised data set. WDNVaR is also less conservative than the traditional ARMA-GARCH VaR.

However, WDNVaR is rejected at higher confidence level 95% across the oil markets in Brent. But given that performance improvement of WDNVaR is based on the wavelet denoising process. The wavelet family and thresholding rule may influence the performance of WDNVaR.

Table 2. Experiments results for ARMA-GARCH VaR

Oil Markets	Confidence level	ARMA(1,1)-GARCH (1,1) VaR Exceedances	Kupiec Test (P-value)	ARMA(1,1)-GARCH (1,1) Acceptance
WTI (West Texas Intermediate)	99%	110	0.6951	√
	97,5%	65	0.1120	√
	95%	44	0.00012	×
Brent	99%	123	0.9573	√
	97,5%	58	0.4315	√
	95%	34	0.0984	√

Table 3. Experiments results for WDNVaR (DB2,2)

Oil Markets	Confidence level	WDNVaR Exceedances	Kupiec Test (P-value)	WDNVaR Model Acceptance
WTI (West Texas Intermediate)	99%	167	0.0641	√
	97,5%	83	0.1362	√
	95%	97	0.1263	√
Brent	99%	210	0.9783	√
	97,5%	87	0.5885	√
	95%	54	0.0334	×

Table 4. Experiments results for WDNVaR (Db2, 3)

Oil Markets	Confidence level	WDNVaR Exceedances	Kupiec Test (P-value)	WDNVaR Model Acceptance
WTI (West Texas Intermediate)	99%	154	0.0813	√
	97,5%	87	0.1121	√
	95%	110	0.1376	√
Brent	99%	197	0.0983	√
	97,5%	87	0.1160	√
	95%	60	0.1275	√

#### 4.6. Experimental Results for WDNVaR(DB2,3)

In this experiment, soft thresholding rule with universal threshold is adopted. Wavelet decomposition level is set at level 3 and Daubechies 2 is chosen as the wavelet family.

Performance improvement brought by WDNVaR is showed in Table 4. Results confirm higher reliability which prove that the heterogeneous market structure is taken into account using wavelet analysis, data and noises are separated and risk evolution is tracked more closely in a multi scale (time scale) domain.

#### 5. Conclusions

Oil markets are getting more volatile and risky with newly emerging characteristics therefore novel risk management techniques are desired. This paper introduces Wavelet Denoising VaR analysis as a promising data smoothing tool for risk measurement and management.

The performance of the proposed WDNVaR and the traditional ARMA-GARCH VaR has been evaluated by Kupiec backtesting procedures.

Unique contributions WDNVaR could offer the multi scale denoising process that increases the goodness of fit in the further modeling attempts Risks are embedded in both data and noises, and thus deserve separate modeling

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