

Improving Accuracy of Educational Research Conclusions by Using Lisrel

Awaluddin Tjalla *

Department of Guidance and Counseling, State University of Jakarta, Kampus UNJ, Jl. Rawamangun Muka, Rawamangun, Jakarta
*Corresponding author: awaluddin.tjalla@yahoo.com

Received February 14, 2015; Revised April 26, 2015; Accepted April 28, 2015

Abstract The purpose of this paper are (1) to propose applying a technique of data analysis of educational variables using LISREL, (2) to construct variables including in the research model. The other benefit of this technique compared to the conventional analysis model are: (1) faulty estimate on variables relation caused by measurement error can be corrected and (2) statistical test on whether or not a theoretical model describing relation structure between variables can be carried out. The other benefit is that fit between theoretical model and data can be tested. The use of LISREL technique to analyze variable data for education is a must. Sharpness and accuracy in predicting the variables which are considered to have influence on variables can be obtained. On the contrary, measurement error which takes place from relation between research variables can be explained. Accordingly, this analysis technique is considered “comprehensive” to improve accuracy of conclusion generalization in the field of educational research which currently undergoes more complex problem.

Keywords: data analysis, educational variables, LISREL technique

Cite This Article: Awaluddin Tjalla, “Improving Accuracy of Educational Research Conclusions by Using Lisrel.” *American Journal of Educational Research*, vol. 3, no. 5 (2015): 619-623. doi: 10.12691/education-3-5-14.

1. Introduction

Globalization which is characterized by advancement in technology has resulted in problems on human life interaction, including those in educational field. In the perspective of research methodology, augmenting problems in educational field either quantitatively or qualitatively require settlement with correct technique of data analysis. This is aimed at obtaining objective result of data analysis and can be generalized accurately. Data analysis in educational field is not as easy as that in the other fields, such as : industry, engineering, agriculture, economics, etc., in which their required statistical analysis can easily be fulfilled. Interpretation made does not bear high risk compared to the more complex data of educational variables. Therefore, correct technique of statistical analysis is required.

Popham and Sirotnik (1973) mentioned two main objectives of statistical use in a bid to analyze variables data in the educational field, they are [19]:

1. Statistical techniques to describe data (descriptive statistics). This statistics is used to infer numerical data, such as : test scores, age and educational year.
2. Statistics used by researchers to describe better inference against a phenomenon observed at sample and then generalized conclusion of population is taken. This analysis technique points to relation between variables. In such case, educational researchers try to describe relation between such variables as students' IQ, achievement and attitude to learning program at school.

With regard to the second objective of using statistics (inferential statistics), the commonly used technique of statistical analysis in the educational field is regression analysis by applying production function approach (Draper and Smith, 1981) [3]. However, such model constitutes underlying weaknesses in terms of : (1) concept, (2) result measurement, and (3) some biased sources which are the characteristics in the educational field. Accordingly, by applying regression with *Ordinary Least Squares* (OLS) approach, such disturbances need serious attention and required assumption can be met. This is because assumption break may cause incorrect and misleading conclusion generalization due to possible misinterpretation (Suriasumantri, 2000) [22].

2. Analysis

Path analysis is commonly applied as well in analyzing educational variables data irrespective of its weaknesses. The following are the weaknesses (Mueller, 1996) [18]: (1) When assumption of series of variables events (one variable cannot precede the other and vice versa) is not met, then path analysis cannot be applied; (2) It is always assumed that error outside the system has no correlation between one and another; (3) Difficulty in determining unknown parameters of the available data; (4) Direction of cause based relation cannot be determined by analysis result but dependent upon the concept developed by researchers. In case of any faulty concept, then conclusion and interpretation will be faulty as well; and (5) Principally, path analysis is the application of equation of

the *Two Stage LeastSquares* (TSLS) which bases as well on the *Ordinary Least Squares* (OLS). Accordingly, when the required assumption by OLS is not fulfilled, then the result will be biased too.

In comparison with regression analysis, path analysis possesses some excellence (James, Mulaik, and Brett, 1982) [6]. This is because we can make influence decomposition of the variables, know how huge the direct and indirect influence as well as that which does not belong to the cause based one. Besides, we can arrange an interesting model on cause based relation between free and tied variables. However, difficulty frequently arises when it comes to making or arranging series of events of such variables.

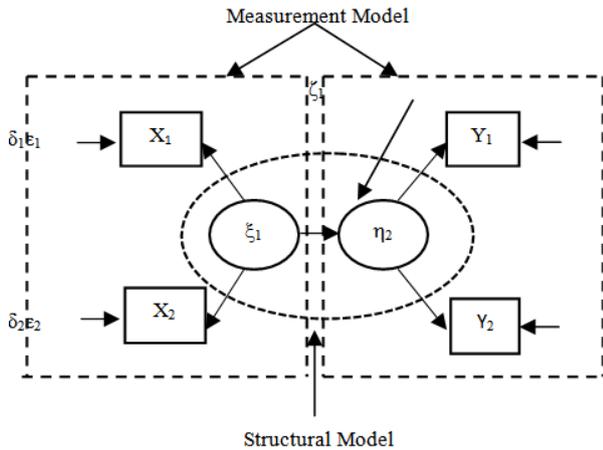


Figure 1. LISREL model consisting of measurement and structural components

At the measurement model analysis, latent variable cannot be directly measured (as a factor or construct, such as children’s spacial ability). Loading at each observed variable for one factor shows correlation between the researched construct and at the common variance with other variable identified as latent variable (Kim and Mueller, 1978) [13].

Equation model used for component of measurement equation is as follows :

1. For measurement equation model x (exogenous model) is :

$$X = \Lambda_x + \delta;$$

$$X = \Lambda_x + \delta;$$

$$\begin{bmatrix} X_1 \\ \vdots \\ X_q \end{bmatrix} = \begin{bmatrix} \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \end{bmatrix} \begin{bmatrix} \xi_1 \\ \vdots \\ \xi_n \end{bmatrix} + \begin{bmatrix} \delta_1 \\ \vdots \\ \delta_q \end{bmatrix}$$

(px1) (pxm) (mx1) (px1)

2. For measurement equation model y (endogenous variable) is as follows :

$$X = \Lambda_y \eta + \varepsilon;$$

$$X = \Lambda_y \eta + \varepsilon;$$

$$\begin{bmatrix} y_1 \\ \vdots \\ y_q \end{bmatrix} = \begin{bmatrix} \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \end{bmatrix} \begin{bmatrix} \eta_1 \\ \vdots \\ \eta_m \end{bmatrix} + \begin{bmatrix} \varepsilon_1 \\ \vdots \\ \varepsilon_q \end{bmatrix}$$

(px1) (pxm) (mx1) (px1)

Where:

- X = vector of measured variable, denoting indicator of latent exogenous variable, ξ .
- Λ_x = loading factor of x variable at a ksi factor.
- ξ = ksi = vector of latent variable.
- δ = delta = vector of unique component (measurement error).
- Y = vector of measured variable, denoting indicator of latent endogenous variable, η .
- Λ_y = Lambda y = loading factor of y variable at a eta factor.
- η = eta = vector of latent variable.
- ε = epsilon = vector of dari unique component (measurement error).

Both of the above measurement equations (for x and y) are the same, showing relation between measured variables x and y with their latent variables (factor to be measured) ξ and η .

Structural equation model points to latent variables analysis (Loehlin, 1992) [15]. This term is used as structural equation model determines relation between latent variables. Notation used for structural equation model is as follows:

$$\eta = B \eta + \Gamma \xi + \zeta$$

$$\eta = B \eta + \Gamma \xi + \zeta$$

$$\begin{bmatrix} \cdot \\ \cdot \\ \cdot \\ \cdot \\ \cdot \\ \eta_m \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} + \begin{bmatrix} \eta_1 \\ \cdot \\ \cdot \\ \cdot \\ \cdot \\ \eta_m \end{bmatrix} + \begin{bmatrix} \text{---} \\ \cdot \\ \cdot \\ \cdot \\ \cdot \\ \cdot \end{bmatrix} \begin{bmatrix} \xi_1 \\ \cdot \\ \cdot \\ \cdot \\ \cdot \\ \xi_n \end{bmatrix} + \begin{bmatrix} \zeta_1 \\ \cdot \\ \cdot \\ \cdot \\ \cdot \\ \zeta_n \end{bmatrix}$$

Where:

- η = vector of endogen latent variable (effect)
- ξ = vector of exogen latent variable (cause)
- ζ = vector of residual variable
- Γ = coefficient matrix describing impact of exogenous variable (ξ) to endogenous variable (η)
- B = coefficient matrix describing impact of endogenous variable (η) to endogenous variable (η).

Basically, structural equation model belongs to equation in the form of matrix of parameters, exogen variables, endogen variables and residual. Detail or element of each matrix is much dependent upon the number of latent variables used and line of cause based relation described. Hence, application of the structural equation highly depends on cause based relation model designed to describe a phenomenon.

Statistically, there are 7 (seven) assumptions to be fulfilled (Mueller, 1996) prior to conducting a test to structural model, they are [18]:

1. Exogenous and endogenous latent variables possess $\bar{X} = 0$; $[E(\xi) = E(\eta) = 0]$;
2. Structural relation of exogenous to endogenous latent variables is linear;
3. Error for ζ at structural equation model: (a) having average same as zero $[E(\zeta) = 0]$; (b) independent, and (c) has no correlation with latent variable $[E(\xi\zeta') = E(\eta\zeta') = 0]$;
4. Matrix $(I - B)$ is not single, a matrix which cannot be inverted.

5. Average of observed variable of the exogeneous and endogeneous variables is 0, that is $E(X) = E(Y) = 0$.
6. Relation between indicators of exogeneous and endogeneous variables and latent variables (either exogeneous or endogeneous) is linear.
7. Error measurement for δ and ϵ in measurement equations x and y : (a) possesses average of 0 [$E(\delta) = E(\epsilon) = 0$]; (b) independent; (c) exogeneous and endogeneous latent variables are not correlated [$E(\xi\delta') = E(\delta\xi') = 0$; $E(\eta\delta') = E(\delta\eta') = 0$; $E(\eta\epsilon') = E(\epsilon\eta') = 0$; and $E(\xi\epsilon') = E(\epsilon\xi')$]; and (d) do not have any correlation between measurement error [$E(\epsilon\delta') = E(\delta\epsilon') = 0$].

In LISREL model there are two stages which are related one another, they are : (1) to test the model truth by seeing whether there exists significant difference between model and data and (2) in case of any accord between model and data, a test of hypothesis on structural relation in such model can be carried out (Hair et.al, 1998) [4]. To test the fit between theoretical model proposed with data a goodness-of-fit test can be applied. This test describes how far the arranged theoretical model is supported by data. Some fit test parameters between model and data cover : Chi-square (χ^2); Indeks Goodness-of-fit (GFI); Indeks Adjusted Goodness-of-Fit (AGFI) and root of residual variance residuor RMR (Byrne, 1998) [2]. In this case data means covariant matrixes between measured variables, they are x and y , and theoretical model is covariant matrixes between x and y which are expected to be secured if the model is correct. Calculation formula of the expected matrixes can be made as each x and y denotes function of latent variables together with their parameters.

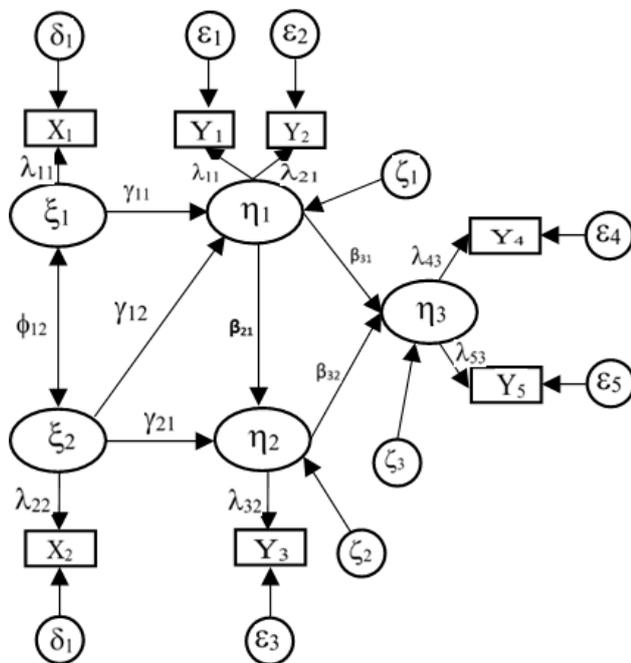


Figure 2. LISREL model on impact of class mixing to learning achievement

In order to obtain a model which is in accord with data, chi-square (χ^2) achieved has to possess probability ≥ 0.05 (Hayduk, 1988) [5]. If zero hypothesis which states that there is no distinction between model with data cannot be rejected (not significant), it means there is no difference

between model and data. In other words, the proposed theoretical model fits to describe data. In furtherance, the fit test between model and data can also be carried out by seeing value magnitude of GFI, AGFI and RMR. The more huge the value of GFI and AGFI obtained (ranging from 0 – 1) and the smaller the value of RMR, it means that the proposed model is good. However, a model test by an index other than *chi-square* (χ^2) is non-probabilistic (cannot be used to determine significance level of the existing difference).

The research is conducted by Maruyama and Miller (1979) [17], in USA by applying LISREL to analyze data from Lewis dan St. John (1974) on influence of class mixing to learning achievement [14]. Reference used is that norms and values possessed by white-skinned students from middle class and achievement oriented will be accepted and internalized by black-skinned students if the white-skinned students are friendly to them. The proposed LISREL model is exhibited at Figure 2.

Remarks :

- = Laten Variable
- ξ_1 = Social economic status
- ξ_2 = % of white-skinned at school
- η_1 = Previous learning achievement
- η_2 = Popularity among white-skinned children
- η_3 = Current learning achievement
- ζ = Faulty measurement of variables equation η and ξ
- δ = Faulty measurement of variable x
- ϵ = Faulty measurement of variable y
- γ = Coefficient which describes the impact of exogenous variable (ξ) to endogenous variable (η)
- β = Coefficient which describes the impact of endogenous variable (η) to exogenous variable (ξ).
- = Observe Variable
- X_1 = Social economic status
- X_2 = % of white-skinned at school
- Y_1 = Intelligence
- Y_2 = Class average score (5)
- Y_3 = Popularity among white-skinned children
- Y_4 = Class average score (6)
- Y_5 = Reading achievement

In furtherance, by applying LISREL as an analysis tool proposed by Maruyama and Miller [17], it is obtained that the value χ^2 is 4,88 and not significant at the significance level of 5 % ($p > \alpha$) with sample of 154 students. This result shows that the proposed LISREL model is fitted with the data. The coefficient magnitude between exogeneous and endogeneous variables as well as between endogeneous and other endogeneous variables is seen at Table 1.

Table 1. Result of Analysis of Stuctural Equation Model on Direct Impact of Exogen Variable to Endogen Variables as well as Endogen Variable to Other Endogen Variable

No.	Parameter	Estimate Value	Interpretation
1.	γ_{11}	.27	Significant
2.	γ_{12}	.29	Significant
3.	γ_{22}	.07	Not significant
4.	β_{21}	.38	Significant
5.	β_{31}	.98	Significant
6.	β_{32}	.02	Not significant
7.	ϕ_{12}	.06	Not significant

Based on the analysis result, it is shown that parameters γ_{11} , γ_{12} , β_{21} and β_{31} are significant, while parameters γ_{22} and β_{32} are not significant. The criteria to determine whether it is or not significant is through estimate value from value $t \geq 1.96$ (Byrne, 1998) [2].

The above analysis result shows that :

1. Family SES (ξ_1) has influence on the previous learning achievement (η_1);
2. Percent age (%) of white-skinned at school (ξ_2) has influence on the previous learning achievement (η_1) and does not influence the popularity of the white-skinned (η_2);
3. The previous learning achievement (η_1) has influence on the current learning achievement (η_3);
4. Popularity among white-skinned (η_2) has no influence on the current learning achievement;
5. There is no significant relation between family SES (ξ_1) and percentage (%) of white-skinned at school (ξ_2).

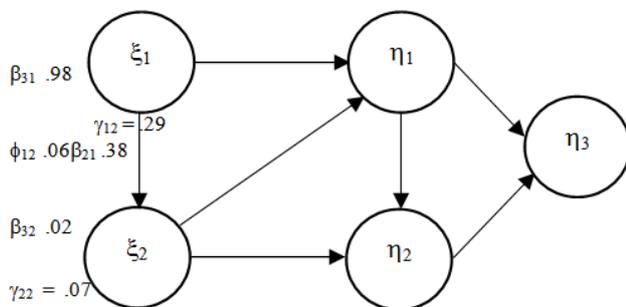


Figure 3. Result of model analysis of structural equation on influence of class mixing to learning achievement

Based on the hypothesis proposed by Maruyama and Miller on transmission of cultural value [17], if correct, then acceptance of black-skinned children by white-skinned children has influence on learning achievement of black-skinned children positively and substantially. However, with insignificant coefficient value at β_{32} (.02), showing that the hypothesis of cultural transmission is not correct and that the previous learning achievement influences the current one and popularity or acceptance by the white-skinned children.

3. Discussion

To overcome the weaknesses in applying analysis techniques, it is proposed to use a model which is currently developed and made popular in a bid to analyze educational variables data known as LISREL (*Linear Structural Relationships*). This analysis technique is also commonly called “analysis of covariance structures, the moments structure model, and latent variable equation systems in structured linear models” (Long, 1983) [16].

This analysis technique belongs to culmination of contemporary methodology (Kerlinger, 1986) [12]. This technique allows inclusion of latent construct variables, in which it cannot be included in regression model and path analysis. The excellence of this model compared to the conventional ones such as regression and path analyses are: (1) estimate error on relation between variables due to measurement error can be well corrected and (2) statistical

test on whether a theoretical model can be accepted or not which describes relation structure between variables can be carried out.

LISREL analysis techniques to examine the fit between the theoretical model with data. In case of no significant distinction between covariant matrix expected based on model or theory and that obtained from data, it can be interpreted as proof of the model’s truth. When a theoretical model supported by data (empirical evidence) has been found, the meaningfulness of each coefficient which is based on cause relation that exists in the model can be tested as well (Joreskog dan Sorbom, 1984) [8].

In LISREL technique, there are two groups of equations (Schumacker and Lomax, 1996) [21], they are measurement and structural equations. The former belongs to factor analysis used for explorative analysis and aimed at stipulating measured variables which can be made as a good indicator for latent variables. In other words, measurement model is made to estimate factor loading for each variable which is theoretically stipulated as an indicator of latent variables or factors. The latter is used to describe cause based relation between latent variables, either between causing variables (exogenous) or between effect variables (endogenous) as well as being used to describe the magnitude of explained and unexplained variances.

4. Conclusion

The use of LISREL in analyzing educational variables is a must as today this analysis model belongs to the most comprehensive one for analysis of behavioral variables. Sharpness and accuracy in predicting variables are considered to have influence on other variables can be executed. In addition, wrong measurement arising out of relation between variables can be explained. Accordingly, this analysis technique is considered “comprehensive” to improve accuracy of conclusion generalization in the field of educational research which currently undergoes more complex problem.

In order to apply LISREL program, supporting knowledge and skill are required as to facilitate us in using this technique. This includes knowledge of mathematics and computer skill besides theoretical mastery to the research model proposed by the researchers.

References

- [1] Britt, David W, A Conceptual introduction to modeling: Qualitative and quantitative perspective. Lawrence Erlbaum Associates, New Jersey, 1997.
- [2] Byrne, Barbara M, Structural equation modeling with LISREL, PRELIS, and SIMPLIS: Basic concepts, applications, and programming, Lawrence Erlbaum Associates, New Jersey, 1998.
- [3] Draper, N. R., and Smith, H., Applied regression analysis (Second edition), John Wiley & Sons, Inc., New York, 1981.
- [4] Hair, Joseph, H., Anderson, Rolph, E., Tatham, Ronald L., and Black, William C, Multivariate data analysis (Fifth edition), Prentice-Hall International, Inc., New Jersey, 1998.
- [5] Hayduk, Leslie A. Structural equation modeling with LISREL. The Johns Hopkins University Press, Maryland, 1988.
- [6] James, Lawrence R., Mulaik, Stanley A., and Brett, Jeanne M, Causal analysis: Assumptions, models, and data, SAGE Publications, Inc., California, 1982.

- [7] Joreskog, Karl G., and Dag Sorbom. *Advances in factor analysis and structural equation models*, Abt Books, Massachusetts, 1979.
- [8] Joreskog, Karl G., and Dag Sorbom, *LISREL VI: Analysis of linear structural relationships by the method of maximum likelihood* (Third Edition), University of Uppsala, Sweden, 1984.
- [9] Joreskog, Karl G., dan Sorbom, Dag, *LISREL 8; User's reference guide*. Scientific Software International, Inc., Chicago, 1996.
- [10] Joreskog, Karl G., Sorbom, Dag., Du toit Stephen, and Mathilda, *LISREL 8: New statistical features*. Scientific Software International, Inc., Chicago, 2000.
- [11] Keith, Timothy Z. *Multiple regression and beyond*. Pearson Education, Inc., Boston, 2006.
- [12] Kerlinger, F.N.. *Foundations of behavioral research* (Third edition), Holt, Rinehart and Winston Inc., Florida, 1986.
- [13] Kim, J., and Mueller, C.W., *Introduction to factor analysis: What it is and how to do it*, SAGE Publications, Inc., Beverly Hills, CA, 1978.
- [14] Lewis, R., and St. John, S., "Contribution of cross-racial friendship to minority group achievement in desegregated classrooms," *Sociometry*, 37, 79-91, 1974.
- [15] Loehlin, John C. *Latent variable models: An introduction to factor, path, and structural analysis*, Lawrence Erlbaum Associates Publishers, New Jersey, 1992.
- [16] Long, Scott J.. *Covariance structure models: An introduction to LISREL*. SAGE Publications Inc., California, 1983.
- [17] Maruyama, G., dan Miller, N., *Reexamination of normative influences processes in desegregated classrooms*. *American Educational Research Journal*, 16, 273-283, 1979.
- [18] Mueller, Ralph O. *Basic principles of structural equation modeling: An introduction to LISREL and EQS*. Springer-Verlag New York, Inc., New York, 1996.
- [19] Popham, James W., dan Sirotnik, Kenneth A. *Educational statistics use and interpretation* (Second edition), Harper & Row, Publishers, Inc, New York, 1973.
- [20] Reisinger, Yvette., dan Turner W, Lindsey. *Cross-cultural behaviour in tourism: Concepts and analysis*. Elsevier Butterworth-Heinemann, Burlington MA, 2003.
- [21] Schumacker, Randall E., dan Lomax, Richard G., *A Beginner's guide to structural equation modeling*, Lawrence Erlbaum Associates, Publishers, New Jersey, 1996.
- [22] Suriasumantri, Jujun S., *Philosophy of science: A popular introduction*, Pustaka Sinar Harapan, Jakarta, 2000.