

Practical Investigation to Improve the Heat Transfer Performance in Elliptical Fins for Different Axis Ratios by Forced Convection

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Abstract All engineering industries have proven that there is a demand to maintain heat transfer and in many engineering production processes, an increase in the rate of thermal transfer is required. The solution lies in adding solid bodies made externally from heat-conducting materials called fins, which in turn have been the subject of very large engineering research by changing shapes, lengths, axis, thicknesses, etc., in order to raise the efficiency of performance in heat transfer to avoid industrial problems and accidents. The materials type and surface area have direct affect of the heat transfer rate depends on the types of materials used and the surface area of the fin. One of the most popular choice is the radial annular fin due to the cylindrical primary surface where the performance of the fins is a function of many parameters, namely the heat transfer coefficient, the fin efficiency and the fins' thermal resistance. In this research work, an experimental study to investigate the effect of fin heat transfer performance characteristics elliptical fin shape at differnt at its major and minor axis ratio (a/b) with different cooling air velocities. As a results, the optimum ratio is found to be for an elliptical shape fins for forced convection.

Keywords: heat transfer performance, natural convection, elliptical fin, and force convection

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1. Introduction

A careful literature review revealed that most of the work done on geometries of the fins is theoretical, and based on thermal and coefficients rather than geometry. Behnia et al. [1] hae theoretical analysis of the heat transfer performance of various commonly used fin geometries in the form of circle, square, rectangle, and ellipse. Results have shown that fins with rounded shapes are better than right angled shapes which is due to the air distribution around the find at low flow, where as squared shapes can generate vortecies around the edges at high speed, and reduce the efficiency. Li et al. [2] have also found that the heat displacement rate is higher with elliptical fin pins in comparison to pin fin and the resistance of the former is lower than the latter expressed in Reynolds number ranging from 1000 to 10,000.

Chapman et al. [3] performed experimental work on using parallel court fins and the fin crossed pins in a low air flow environment and compare these fins with an elliptical pin fin heat sink. A heat sink of the same volume in their experiment are used which concluded that the overall thermal resistance of the parallel plate fin is lower than the other two designs, on the other hand, the elliptical

pin fins shown higher heat transfer coefficient. Ota et al. [4,5] have practically investigated the heat transfer and its flow around oval cylinder with axes in proportions of 1:2 and 1:3. The results show that the heat transfer coefficient of the oval cylinder is higher than the heat transfer coefficient of the circular cylinder with equal circumference and that the pressure drawing coefficients for the first is less than the previous ones. Poulidakos and Bejan [6] build a theoretical framework to explain the effect of entropy on fin dimensional variation and whether there are optimum dimensions when heat transfer by forced convection. First they developed an expression for a general fin entropy generation rate and then applied it to determine the optimum dimensions for pin fins, rectangular plate fins, trapezoidal fins, and triangular fins of rectangular cross section. It does not seem that in their studies anything added to engineering industries distinguishes them from others. Jonsson and Bjorn [7] have compared experimental results to find the thermal performance of heat platters using different fin designs such as straight and pin fins with circular, quadratic and elliptical cross sections. They have evaluated the thermal performance by comparing the heat resistance of heat exchangers by decreasing pressure at a constant velocity. They recommended the use of elliptical pin fins at high speeds and round pin fins at medium range speeds. Wirtz et. al. [8] they reached

experimental results on the heat transfer performance of the pin-fin fan pool assemblies used different pin -fins shape like diamond ,cylindrical, and square and found that cylindrical pin-fins give the best overall heat transfer performance.

Laor and Kalman [9] studies the effect of heat generation on the performance of longitudinal fins, spines, and ring fins of equivalent, rectangular and triangular shapes with regular and irregular temperature distributions observed, while Mokheimer and Esmail [10] locally examined the performance of ring fins for different profiles subject to a variable heat transfer coefficient. This study is developed by studying the end wall heat transfer and total pressure drop measurements for elliptical pin fin arrays performed by Uzol and Camci [11].

Nagarani and Mayilsamy have investigated circular and ring fins and found that these are one of the most widely used options for exchanging heat. They found that the rate and efficiency of heat transfer of circular and oval ring fins were analyzed for several different environmental variables. The efficiency of the elliptical fin is more than the ring fin, if there is a restriction of space in a certain direction for the length while the vertical direction is relatively unconstrained, in practice the elliptical fin is a good choice [12].

Practical result by Al-Jawaree [13] proved that the surface temperature of elliptical fin decreased with increase in fin length along major axis. Three fins shape, namely elliptical, circular and diamond were used to investigate the heat transfer performance at natural convection and it is found the elliptical fin shape had more heat transfer performance than other shape used [14]. In addition, extended to this work, the influence of elliptical fin axis ratio to the fin heat transfer performance was examined at free convection [15].

2. Experimental Methods

In this work, natural and forced convection heat transfer of elliptical annular fins with different length depth ratios are experimentally investigated. Eight specimens sets with elliptical annular fin and cross section with different axis aspect ratios (a/b) are used. The following ratios are used: 2.0, 2.21, 2.44, 2.65, 2.88, 3.13, 3.38 and 3.65. All the specimens are of the same surface area and thickness as shown in Figure 1. For examining the forced convection, it is decided to use the air flow velocity from 0.15 to 0.28 m/s.



Figure 1. Elliptical fin shape at different axis used in the experimental work for natural convection

The materials used in this experimental work is AA6061 aluminium alloy due to its good thermal conductivity, low price and low density. The material physical parameters are: thermo-physical properties = 2719 kg/m^3 , $C_p = 871 \text{ J/kg K}$, $K = 233 \text{ W/m K}$. The specifications of elliptical fin and the experimental rig are listed in Table 1 and shown in Figure 2.

Table 1. Specification of fins and heat exchanger

Testing rig specifications	
Fin material	AA6061
Fin thickness	1 mm
Heater type	Tubular
Heater temperature controller	PID using J type thermocouple
Material of circular pipe	Stainless steel
Pipe thickness	1 mm
Pipe diameter	19 mm
Pipe length	800 mm
Variation of heat temperature between switching	$2 \text{ }^\circ\text{C} \pm$
Heater voltage	220 Volts AC



Figure 2. The experimental rig used for natural convection

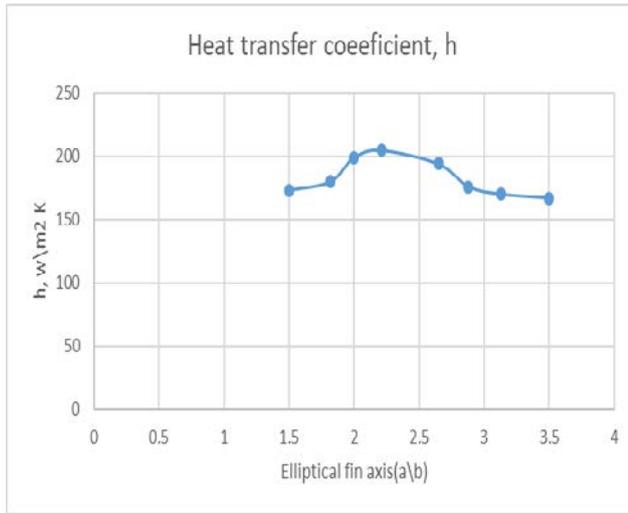
The following assumptions are made during the experimental work: the fins are of homogeneous materials. The temperature around the fins are uniform, the fins' thickness is small in comparison to the dimension, hence the temperature gradient allows for the edge of the fin to be neglected. The base tube's temperature is uniform, and no heat transfer occurs during the experiment.

3. Results and Discussions

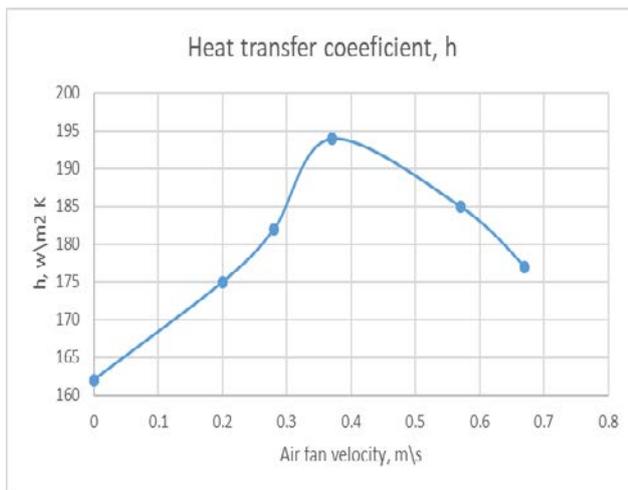
The heat transfer coefficient is one of the important factors in this work, the heat transfer from the fin to the surrounding atmosphere is affected by the air velocity and the aspect ratio of the fins. The results in Table 2 show that set No. 4 ($a/b = 2.65$) has a higher value of heat transfer coefficient to the temperatures used about $162 \text{ W/m}^2 \text{ K}$ by free convection [15], hence the axis aspect ratio of elliptical fin was fixed for practical examination as summarised in Table 2. In addition, the table shows the heat transfer coefficient result with change of fin aspect ratio at constant air fan velocity ($V = 0.37 \text{ m/s}$) is summarised.

Table 2. The heat transfer coefficient at a different axis ratio by forced convection

a/b ratio	h (w/m ² K)	Air velocity (m/s)	h (w/m ² K)
1.50	173	0.00	162
1.82	180	0.20	175
2.00	199	0.28	182
2.21	205	0.37	194
2.65	194	0.57	185
2.88	176	0.67	177
3.13	170		
3.50	167		

**Figure 3.** Coefficient of heat transfer at different elliptical fin aspect ratios

The heat transfer coefficient has a high values at elliptical fin aspect ratio (a/b) between 2 to 2.65, this will lead possibility to found the optimum axis ratio in this range. The heat transfer coefficient has range from 160 to 200 w/m² K for this research work.

**Figure 4.** Coefficient of Heat transfer at different air fan velocities

It can be deduce from the above figure the highest value of heat transfer coefficient at 0.37 m/s fan air speed due to a good temperature distribution and heat transfer rate from the fins surface.

The fin heat transfer rate (Q_{fin}) is calculated for different fin aspect ratios and air fan velocities at constant temperatures (100°C) and cross section area. The fin heat transfer rate can be estimated using equation 1 [15].

$$Q_{fin} = M \times \tanh(mL) \quad (1)$$

where $M = \sqrt{h \times p \times k \times A_c} (T_b - T_\infty)$

$$mL = \sqrt{\frac{h \times p}{k \times A_c}} \times L \quad (2)$$

where p is the fin perimeter, k is the thermal conductivity, A_c is the cross sectional area of the fin, and L is the length of the fin.

The fin heat transfer performance is measured by estimating the fin effectiveness (E_f), the fin efficiency (η_f) and overall fin thermal resistance (R_o). Hence, it has been decided to separately calculate each individual parameter. The heat transfer coefficient (h , w/m² K) can be estimated from equations 3 and 4 [16,17].

$$h = \frac{Q_{fin}}{A_f (T_b - T_\infty)} \quad (3)$$

where Q_{fin} is the heat transfer from the fin surface at T_s , A_f is the total fin surface area, and T_∞ is the ambient temperatures.

The fin efficiency (η_{fin}) is defined as:

$$\eta_{fin} = \frac{Q_{fin}}{Q_{fin_max}} \quad (4)$$

$$= \frac{\text{Actual heat transfer rate from the fin}}{\text{Ideal heat transfer rate from the fin}}$$

This relationship enables us to determine the heat transfer from a fin when its efficiency is known. But the overall fins efficiency (η_o) is expressed by equation 5.

$$\eta_o = 1 - \left(\frac{A_{fin}}{A_t} \right) (1 - \eta_{fin}) \quad (5)$$

The performance of fins expressed in term of the fin effectiveness ϵ_f is defined as:

$$\epsilon_f = \frac{q_f}{h A_{c,b} \theta_b} \quad (6)$$

where $A_{c,b}$ is the surface area of fins array on the base (m²), θ_b is the temperature difference ($T_b - T_s$) and T_b is the temperature of heated surface.

The fin thermal resistance (R_{fin}) expressed in units of (°C/W) is defined as temperature rise per unit of power. Based on the device dissipation, the total thermal resistance can be calculated as expressed by equation 7 [18,19].

$$R_o = \frac{1}{h \times A_f \times \eta_f} \quad (7)$$

where A_f is the fin surface area (m²), and η_f is the fin efficiency. Equation 7 is used to calculate the thermal resistance of the fins array. A small fraction of thermal resistance in an indication to a small temperature drop across the heat sink. Hence, fins with high thermal efficiency accounts of heat flow paths for conduction-convection in the fins and convection from the prime surface. Hence, in order to study the effect of the elliptical

fin axis ratio by force convection to the fin heat transfer performance, the above three parameters were calculated at the wide range of elliptical fin axis ratio using equation 7.

Actually, the experimental works divided in two parts, the first part examination of air fan velocities to the constant fin axis ratio ($a/b = 2.65$) and the results summarized in Table 3. But the second part of this research work done at a constant fan air velocity ($V = 0.37$ m/s) with a wide range of elliptical fin axis ratio, this is because an average velocity found at part one of this research work and the results are summarized in Table 4. The experiments were done at constant temperature in air surroundings excluding air currents at constant surface area for the elliptical fin (0.0395 m^2) for all sets used. Hence, in order to achieve the above point elliptical fin axis ratio fixed at ($a/b = 2.65$) with a wide range of fan air velocities, this is because an optimum axis ratio found at free convection work. Free convection experimental results done at an air velocity equal to zero measuring the enhance of fin heat transfer performance by using the force convection. The results of the part one are illustrated in Table 3.

Table 3. Elliptical Fin heat transfer performance by force convection.

Convection	V (m/s)	ϵ	η	η_o	Ro
Natural	0.00	1.34	0.335	0.524	0.115
Forced	0.2	3.85	0.85	0.953	0.09
Forced	0.28	3.76	0.78	0.947	0.094
Forced	0.37	3.72	0.68	0.941	0.098
Forced	0.57	3.65	0.63	0.936	0.1
Forced	0.65	3.57	0.6	0.933	0.103
Forced (Avg.)		3.71	0.708	0.942	0.097

The fin heat transfer performance of elliptical fin at force convection is illustrated in Figure 5, Figure 6, and Figure 7. The fin effectiveness increase at air fan velocity equal 0.2 m/s and then slightly decrease with increase the air velocity due to lower thermal distribution zone area on the fin surface happen at high velocities.

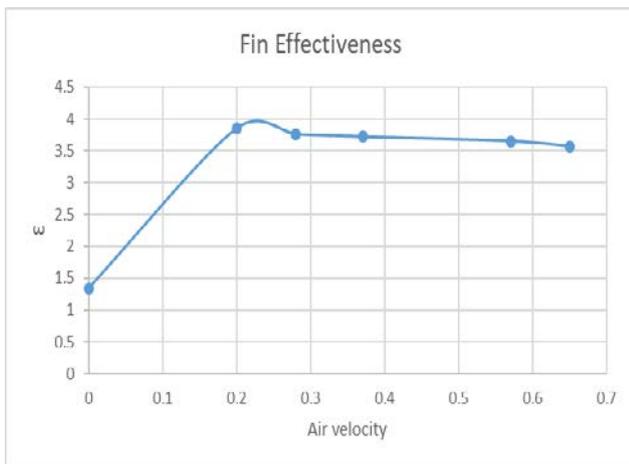


Figure 5. Elliptical fins effectiveness (ϵ) with air fan velocities

It can be deduced from Figure 5 that all the values of fins effectiveness are more than one. This means an enhance of heat transfer rate from the fins surface for all sets used in this work. The range of fin effectiveness is

from 3.2 to 3.85. The enhance the percentage by used the force convection instead the free convection can be calculated using equation 8.

$$\text{Improvements (\%)} = \frac{\text{Force convection effect} - \text{Free convection effect}}{\text{Free convection fin effect}} \times 100\% \quad (8)$$

This increment reaches to 177%, while the enhance percentage of overall fin efficiency raise of 80% for force convection than used for free convection at fan air velocity is equal to zero as shown in Figure 6 and Figure 7.



Figure 6. Elliptical fin efficiency (η) with air fan velocities

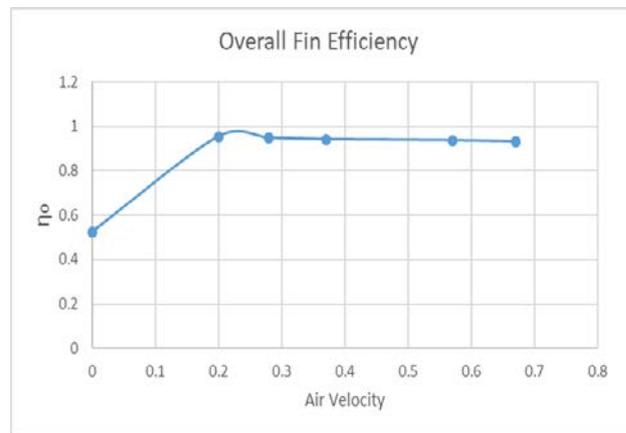


Figure 7. Overall Elliptical fin efficiency (η_o) with air fan velocities

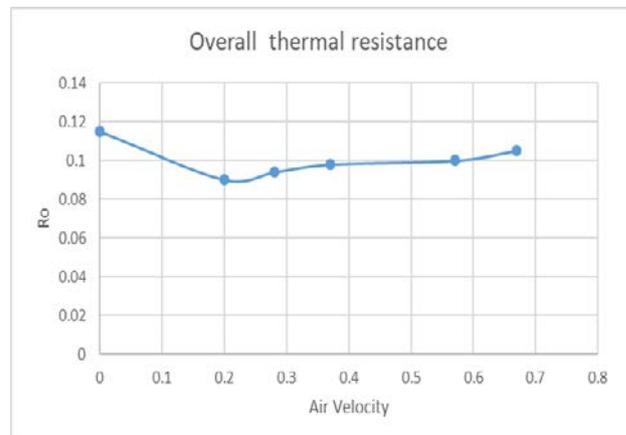


Figure 8. Elliptical overall thermal resistance (R_o) with air fan velocities

The results of overall efficiency conforms the fin efficiency for all air fan velocity used. At 0.2 m/s air velocity a high value of fins efficiency and lower overall thermal resistance, this is mean a high fin heat transfer performance found, with the constant elliptical fin axis ratio of $a/b = 2.65$.

To examine the effects of elliptical fin axis ratios to the fin heat transfer performance, the experimental work done at a constant fan velocity 0.37 m/s, temperature 100°C, 8 fis with surface area of 0.0396 m² and wide range of elliptical fin aspect ratios from 1.5 to 3.5. The results of this part are summarised in Table 4 and illustrated in Figure 9 - Figure 12.

Table 4. The effects the elliptical fin axis ratio the fin heat transfer performance

a/b ratio	Ro (°C/w)	ϵ	η	η_o
1.5	0.1206	3.21	0.55	0.908
1.82	0.1058	3.47	0.62	0.916
2	0.0921	3.75	0.69	0.953
2.21	0.0885	3.85	0.73	0.965
2.65	0.0944	3.69	0.67	0.941
2.88	0.0965	3.64	0.65	0.936
3.13	0.0971	3.57	0.63	0.928
3.5	0.0987	3.44	0.62	0.915

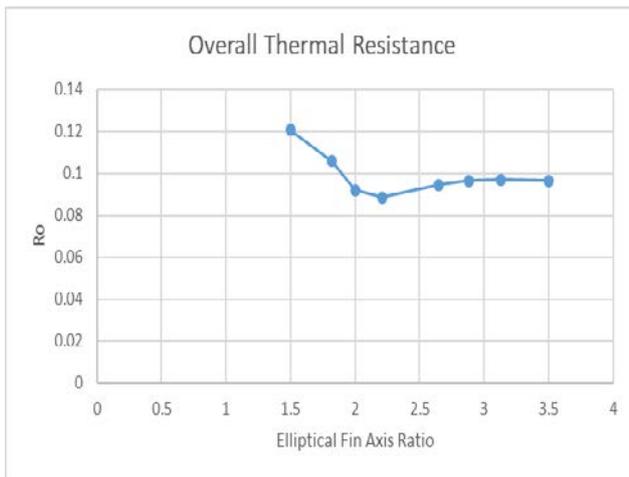


Figure 9. Overall thermal resistance with different elliptical fin aspect ratios

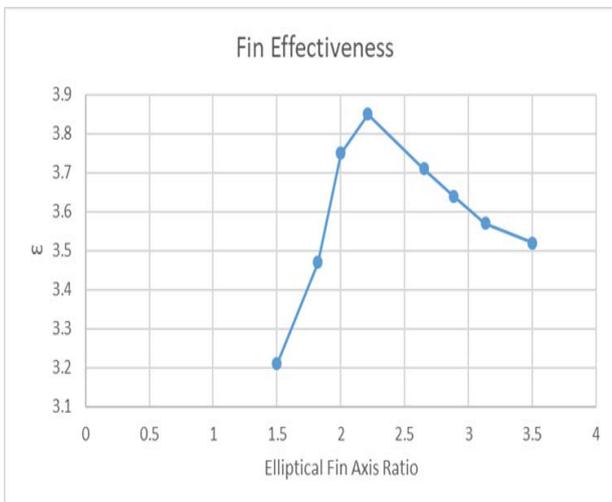


Figure 10. Fins effectiveness (ϵ) with different elliptical fin aspect ratios

It can be deduced from the above figure; all the values of fin effectiveness are more than one. So, this means an enhance of heat transfer rate from the fins surface happen for all axis ratio used in this work. The range of fin effectiveness is from 3.2 to 3.85. The fin efficiency has the range from 55 % to 75 %, but the overall fin efficiency range from 90 to 96 % due excellent design operation heat transfer fins system.

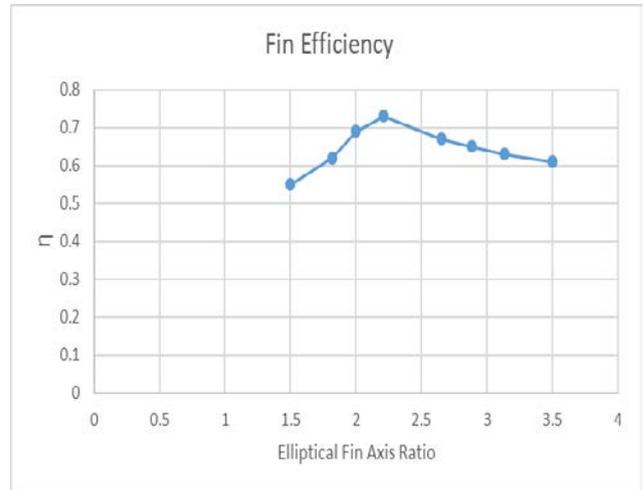


Figure 11. Fin efficiency with different elliptical fin axis ratio

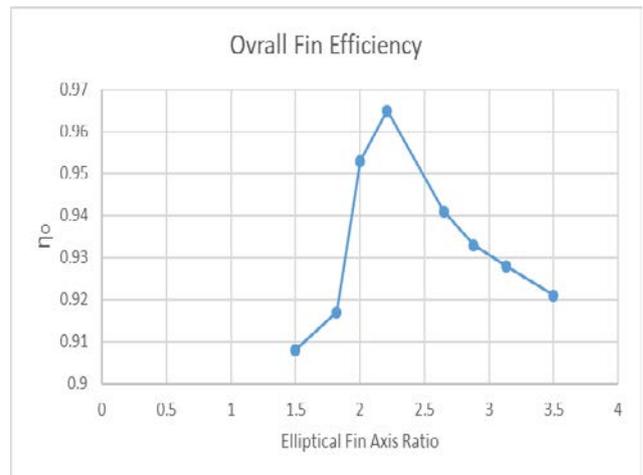


Figure 12. Overall fin efficiency with different elliptical fin axis ratio

It can be deduce from Figure 9, Figure 10, Figure 11 & Figure 12 that set No. 4 ($a/b = 2.21$) has the highest efficiency and effectiveness and the least forced convection thermal resistance. While set No. 1 ($a/b = 1.5$) has a lowest value of heat transfer due to a large thermal distraction in the fin surface. The fins aspect ratios are very effects the fin heat transfer performance.

4. Conclusion

The results show that the elliptical annular fin with many axis ratios are effect the heat transfer performance of fin by both natural and force convection. The experimental results were fitted to deduce empirical correlations for force convection test. It is also found an optimum aspect ratio of 2.65 of the elliptical fin at has a high performance of heat transfer by free convection.

So, this axis ratio fixed at practical studying the variation of air fan velocities. Considering the above points, it is concluded that the heat transfer rate of elliptical fins is better with respect to the heat transfer coefficient, shaped tube efficiency, thermal resistance, overall efficiency and effectiveness when the range of different major and minor axis ratio between 2 to 2.65. The overall fin efficiency range is from 90 to 96 % and the fin effectiveness more than one with the major and minor axis ratios and expect an increase with increasing the number of fins. While the enhance of fin heat transfer performance has a range from 80 to 180 % for this research work.

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